

### Problem 1

For each of the following states of a particle in a three-dimensional box, at what points is the probability distribution function a maximum?

- (a)  $n_x = 1, n_y = 1, n_z = 1$ .
- (b)  $n_x = 2, n_y = 2, n_z = 1$ .

### Problem 2

For a particle in a three-dimensional box, what is the degeneracy (number of different quantum states with the same energy) of the following energy levels?

- (a)  $\frac{3\pi^2\hbar^2}{2mL^2}$ .
- (b)  $\frac{9\pi^2\hbar^2}{2mL^2}$ .

### Problem 3

- (a) How many different 5g states does hydrogen have?
- (b) Which of the 5g states has the largest angle between  $\vec{L}$  and the z-axis, and what is that angle?
- (c) Which of the 5g states has the smallest angle between  $\vec{L}$  and the z-axis, and what is that angle?

### Problem 4

The 1s wavefunction for hydrogen is  $\psi_{1s}(r) = \frac{1}{\sqrt{\pi a^3}} e^{-r/a}$ . The probability of finding the electron in the 1s state between the radii  $r_1$  and  $r_2$  is determined by  $P(r_1 \leq r \leq r_2) = \int_{r_1}^{r_2} |\psi_{1s}(r)|^2 4\pi r^2 dr$

- (a) What is the probability that an electron in the 1s state of a hydrogen atom will be found at a distance less than  $a/2$  from the nucleus?
- (b) Calculate the probability that the electron will be found at distances between  $a/2$  and  $a$  from the nucleus.

### Problem 5

A hydrogen atom is in a  $d$  state. In the absence of an external magnetic field the states with different  $m_l$  values have (approximately) the same energy. Consider the interaction of the magnetic field with the atom's orbital magnetic dipole moment.

- (a) Calculate the splitting (in electron volts) of the  $m_l$  levels when the atom is put in a 0.400 T magnetic field that is in the  $+z$  direction.
- (b) Which  $m_l$  level will have the lowest energy?
- (c) Draw an energy-level diagram that shows the  $d$  levels **with** and **without** the external magnetic field.

### Problem 6

Calculate the energy difference between the  $m_s = \frac{1}{2}$  ("spin up") and  $m_s = -\frac{1}{2}$  ("spin down") levels of a hydrogen atom in the 1s state when it is placed in a 1.45 T magnetic field in the  $-z$  direction.

### Problem 7

- (a) Write out the ground-state electron configuration ( $1s^2, 2s^2, \dots$ ) for the carbon atom.
- (b) What element of next-larger  $Z$  has chemical properties similar to those of carbon?
- (c) Give the ground-state electron configuration for the element in part (b).

### Problem 8

Estimate the energy of the highest  $l$  state for

- (a) the  $L$  shell of  $\text{Be}^+$ ,
- (b) the  $N$  shell of  $\text{Ca}^+$ .

### Problem 9

The energies for an electron in the  $K$ ,  $L$ , and  $M$  shells of the tungsten atom are  $-69.5$  keV,  $-12.0$  keV, and  $-2.20$  keV respectively. Calculate the wavelengths of the  $\alpha$  and  $\beta$  x rays of tungsten.

### Problem 10

Rydberg atoms are atoms whose outermost electron is in an excited state with a very large principal quantum number. Rydberg atoms have been produced in the laboratory and detected in interstellar space.

- (a) Explain why all neutral Rydberg atoms with the *same principal quantum number*  $n$  have essentially the same ionization energy, independent of the total number of electrons in the atom.
- (b) What is the ionization energy for a Rydberg atom with a principal quantum number of  $n = 350$ ?
- (c) What is the radius in the Bohr model of the Rydberg electron's orbit when  $n = 350$ ?
- (d) What is the ionization energy for a Rydberg atom with a principal quantum number of  $n = 650$ ?
- (e) What is the radius in the Bohr model of the Rydberg electron's orbit when  $n = 650$ ?

### Problem 11

If the value of  $L_z$  is known, we cannot know either  $L_x$  or  $L_y$  precisely, but we can know the value of the quantity  $\sqrt{L_x^2 + L_y^2}$ . Write an expression for this quantity in terms of  $l$ ,  $m_l$ , and  $\hbar$ .

- (b) What is the meaning of  $\sqrt{L_x^2 + L_y^2}$ ?
- (c) For a state of nonzero orbital angular momentum, find the maximum and minimum values of  $\sqrt{L_x^2 + L_y^2}$ .